

Structure of TCE

So Hirata

Pacific Northwest National Laboratory

This presentation will address

- ◆ How TCE works
- ◆ How TCE-generated programs work
- ◆ How TCE can be used
- ◆ How TCE can be enhanced
- ◆ Other sources of information

How TCE works — overview

- ◆ TCE derives working equations for a second quantized many-electron theory
 - TCE is written in Python[®] programming language
- ◆ TCE implements the working equations into parallel programs
 - For the NWChem[©] QC software suite
 - Using ParSoft[©] Library

How TCE works — supported models

$$\langle Q | [(L_0 + L_1 + \dots)(H_1 + H_2) \exp(T_1 + T_2 + \dots)(R_0 + R_1 + \dots)]_{C/L} | P \rangle$$

◆ CISD $\langle D | (H_1 + H_2)(R_1 + R_2) | O \rangle = E \langle D | (R_1 + R_2) | O \rangle$

◆ MBPT(2) $\langle D | (H_1)(R_1 + R_2) | O \rangle + \langle D | (H_2) | O \rangle = 0$

◆ CCSDT $\langle T | [(H_1 + H_2) \exp(T_1 + T_2 + T_3)]_C | O \rangle = 0$

◆ EOM-CCSD $\langle D | [(H_1 + H_2) \exp(T_1 + T_2)(R_1 + R_1)]_C | O \rangle = 0$

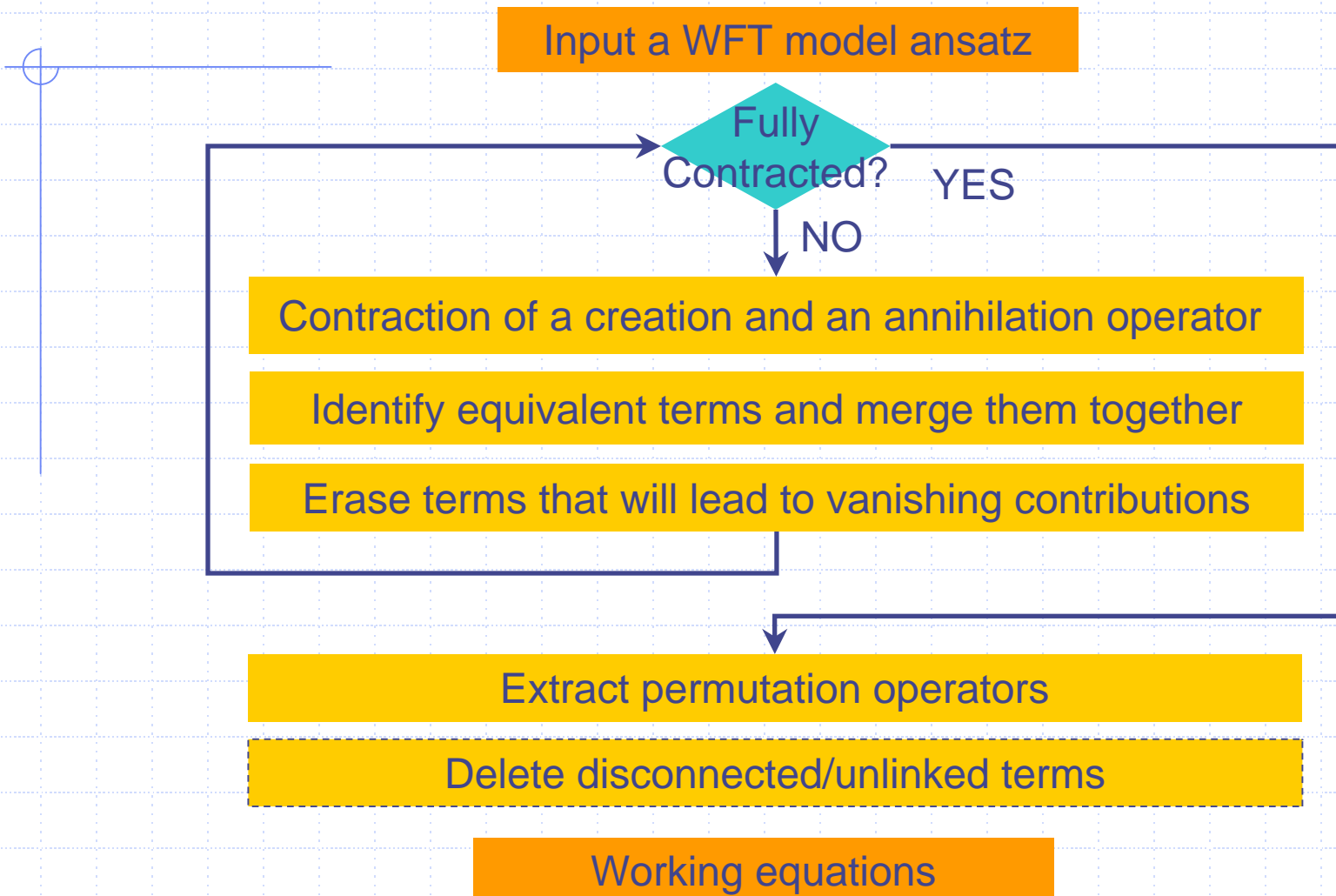
◆ CCSD lambda equation

$$\langle O | [(1 + L_1 + L_2)[(H_1 + H_2) \exp(T_1 + T_2)]_C]_L | D \rangle = 0$$

◆ CCSD dipole moments

$$\langle O | (1 + L_1 + L_2)[(H_1) \exp(T_1 + T_2)]_C | O \rangle = \langle H_1 \rangle$$

How TCE works — formula derivation



How TCE works — program synthesis

Input WFT working equations

Strength reduction: $X=ABCD \rightarrow X=((BC)A)D$

Factorization: $X=AB+AC \rightarrow X=A(B+C)$

Intermediate reuse: $X=AB+C(AB) \rightarrow Y=AB, X=Y+CY$

Operation Tree

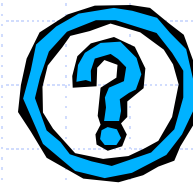
Determine permutation symmetry of intermediates

Analyze the use of permutation symmetry in contraction

Generate Fortran77/Fortran90 programs

How TCE-generated programs work — challenges

- ◆ Use of spin & spatial symmetry in tensor storage & contraction
- ◆ Use of permutation symmetry in tensor storage & contraction
- ◆ Permutation symmetry of intermediates
- ◆ Abstraction of theories
- ◆ Memory management
- ◆ Scalability to massively parallel regime



How TCE-generated programs work

— permutation symmetry

◆ Reduced storage size

$$t_{ij}^{ab} \Rightarrow t_{i<j}^{a<b}$$

◆ Reduced operation cost

$$\sum_{cd} t_{ij}^{cd} v_{cd}^{ab} \Rightarrow 2 \sum_{c<d} t_{i<j}^{c<d} v_{c<d}^{a<b}$$

How TCE-generated programs work — intermediates

◆ With no de-excitation (L) operator

$$i \cdot g_1 < g_2 < g_3 < \dots < g_n, l_1 < l_2 < l_3 < \dots < l_p \\ g'_1 < g'_2 < g'_3 < \dots < g'_m, l'_1 < l'_2 < l'_3 < \dots < l'_q$$

◆ With a de-excitation (L) operator

$$i \cdot g_1 < g_2 < g_3 < \dots < g_n, h_1 < h_2 < h_3 < \dots < h_p, p_1 < p_2 < p_3 < \dots < p_p \\ g'_1 < g'_2 < g'_3 < \dots < g'_m, h'_1 < h'_2 < h'_3 < \dots < h'_q, p'_1 < p'_2 < p'_3 < \dots < p'_q$$

How TCE-generated programs work — spin & spatial symmetries

◆ Spin symmetry

$$\begin{array}{ccc} \text{Covariant} & & \text{Contravariant} \\ \text{indices} & & \text{indices} \\ \sum_p S_p & = & \sum_q S_q \end{array}$$

◆ Spatial symmetry

$$\prod_p \Gamma_p = \Gamma_0$$

How TCE-generated programs work — tiling algorithm

```
DO i
  DO j
    IF (i>j)
      IF X(ij) IS NONZERO
        ARITHMETIC
```

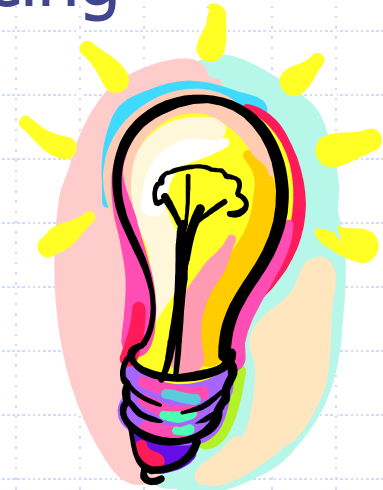
IF	IF	IF	IF	IF	IF	IF	IF
IF	IF	IF	IF	IF	IF	IF	IF
IF	IF	IF	IF	IF	IF	IF	IF
IF	IF	IF	IF	IF	IF	IF	IF
IF	IF	IF	IF	IF	IF	IF	IF
IF	IF	IF	IF	IF	IF	IF	IF
IF	IF	IF	IF	IF	IF	IF	IF
IF	IF	IF	IF	IF	IF	IF	IF

```
DO I (i1~i2)
  DO J (j1~j2)
    IF (I>J)
      IF X(IJ) IS NONZERO
        DO i
          DO j
            ARITHMETIC
```

IF	IF	IF	IF
IF	IF	IF	IF
IF	IF	IF	IF
IF	IF	IF	IF

How TCE-generated programs work — tiling algorithm

- ◆ Spin, spatial, and permutation symmetries
- ◆ Near-operation-minimum
- ◆ Runtime adjustment of peak memory size
- ◆ Granularity of dynamic load balancing parallelism



How TCE can be used — preliminary

- ◆ Use a Windows or LINUX machine
- ◆ Download the latest Python® from www.python.org (free)
 - TCE codes (aee.py, ccc.py, oce.py, tce.py) will run
- ◆ Obtain the latest NWChem development version for interfacing and running the TCE-generated codes
 - Minor modification of TCE's code generator & development of interface will permit other QC software suites than NWChem

How TCE can be used — text based

cf) Auer's presentation

```
Shortcut to python.exe
Python 2.2.1 (#34, Apr 9 2002, 19:34:33) [MSC 32 bit (Intel)] on win32
Type "help", "copyright", "credits" or "license" for more information.
>>> import oce
>>> ccd_t2 = oce.readfromfile("ccd_t2.in")
>>> print ccd_t2

[ + 0.25 1 * Sum < g5 g6 g7 g8 > * v < g5 g6 g7 g8 > * <0! < h1+ h2+ p4 p3 > < g5+ g6+ g8 g7 > !0>
[ + 0.25 1 * Sum < g5 g6 p7 p8 h9 h10 > * f < g5 g6 > * t < p7 p8 h9 h10 > * <0! < h1+ h2+ p4 p3 > < g5+ g6 >
< p7+ p8+ h10 h9 > !0>
[ + 0.0625 1 * Sum < g5 g6 g7 g8 p9 p10 h11 h12 > * v < g5 g6 g7 g8 > * t < p9 p10 h11 h12 > * <0! < h1+ h2+ p
4 p3 > < g5+ g6+ g8 g7 > < p9+ p10+ h12 h11 > !0>
[ + 0.0078125 1 * Sum < g5 g6 g7 g8 p9 p10 h11 h12 p13 p14 h15 h16 > * v < g5 g6 g7 g8 > * t < p9 p10 h11 h12
> * t < p13 p14 h15 h16 > * <0! < h1+ h2+ p4 p3 > < g5+ g6+ g8 g7 > < p9+ p10+ h12 h11 > < p13+ p14+ h16 h15 >
!0>

>>> ccd_t2 = ccd_t2.performfullcontraction()
[ + 0.25 1 * Sum < g5 g6 g7 g8 > * v < g5 g6 g7 g8 > * <0! < h1+ h2+ p4 p3 > < g5+ g6+ g8 g7 > !0>
... commencing full operator contraction
... iteration = 1, number of terms = 1
... iteration = 2, number of terms = 1
... iteration = 3, number of terms = 1
... iteration = 4, number of terms = 1
[ + 0.25 1 * Sum < h9 h10 p7 p8 g5 g6 > * f < g5 g6 > * t < p7 p8 h9 h10 > * <0! < h1+ h2+ p4 p3 > < g5+ g6 >
< p7+ p8+ h10 h9 > !0>
... commencing full operator contraction
... iteration = 1, number of terms = 2
... iteration = 2, number of terms = 3
... iteration = 3, number of terms = 6
... iteration = 4, number of terms = 7
... iteration = 5, number of terms = 4
[ + 0.0625 1 * Sum < h7 h8 p5 p6 g9 g10 g11 g12 > * t < p5 p6 h7 h8 > * v < g9 g10 g11 g12 > * <0! < h1+ h2+ p
4 p3 > < g9+ g10+ g12 g11 > < p5+ p6+ h8 h7 > !0>
... commencing full operator contraction
... iteration = 1, number of terms = 2
... iteration = 2, number of terms = 4
... iteration = 3, number of terms = 8
... iteration = 4, number of terms = 14
... iteration = 5, number of terms = 10
... iteration = 6, number of terms = 6
[ + 0.0078125 1 * Sum < h7 h8 h11 h12 p5 p6 p9 p10 g13 g14 g15 g16 > * t < p5 p6 h7 h8 > * t < p9 p10 h11 h12
> * v < g13 g14 g15 g16 > * <0! < h1+ h2+ p4 p3 > < g13+ g14+ g16 g15 > < p5+ p6+ h8 h7 > < p9+ p10+ h12 h11 >
!0>
... commencing full operator contraction
... iteration = 1, number of terms = 3
... iteration = 2, number of terms = 6
... iteration = 3, number of terms = 12
... iteration = 4, number of terms = 23
... iteration = 5, number of terms = 28
... iteration = 6, number of terms = 12
... iteration = 7, number of terms = 16
... iteration = 8, number of terms = 8
>>> print ccd_t2

[ + 1.0 1 * v < p3 p4 h1 h2 >
[ - 1.0 1 * Sum < h5 > * f < h5 h1 > * t < p3 p4 h5 h2 >
[ + 1.0 1 * Sum < h5 > * f < h5 h2 > * t < p3 p4 h5 h1 >
```

How TCE can be enhanced — limitations of TCE

◆ Tested for ...

- CC up to CCSDTQ, CI up to CISDTQ, 'generalized' MBPT up to MBPT(4), CC \wedge up to CCSDTQ, EOM-CC (right & left) up to EOM-CCSDTQ

◆ Anything else will probably need some work

- But far less than a full manual implementation would!
- cf) Sadayappan's presentation

How TCE can be enhanced — collaborations

◆ Join our effort!

- Partner with existing members (quantum chemists or computer scientists) to realize your new methods much more quickly
- ex) **Professor Rodney Bartlett & Mr. Igor Schweigert** — CC analytical derivatives
- ex) **Professor Piotr Piecuch, Dr. Karol Kowalski, Professor Mark S. Gordon** — Novel CC & EOM-CC methods
- ex) **Professor Kimihiko Hirao, Dr. Takeshi Yanai** — Relativistic correlation theories

Other sources of information

◆ Papers

- G. Baumgartner *et al.* Proc. Supercomp. (2002) [Performance optimization aspects]
- D. Cociorva *et al.* Lect. Notes Comput. Sci. **2228**, 237 (2001). [Performance optimization aspects]
- S. Hirata, J.Phys.Chem.A **107**, 9887 (2003) [TCE specs, and CISDTQ, CCSDTQ, MBPT(4) applications]
- S. Hirata *et al.*, J.Chem.Phys. **120**, 3297 (2004) [DK3 relativistic CCSDTQ applications]
- S. Hirata, submitted [EOM-CCSDTQ applications]

◆ Webpage

- <http://www.cis.ohio-state.edu/~gb/TCE/>

◆ TCE Manual

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