Logic Programming

Textbook, Ch. 14

Logic Programming

- Instead of using functions as in imperative and functional programs
- We use predicates, as in predicate calculus
- Interpretation = proving theorems

Prolog

- Developed at Univ. of Aix-Marseille and Edinburgh in early to mid 1970s
- Goal: natural language processing and theorem proving
- Used in Japan’s Fifth Generation Computing Project in 1981
Prolog Syntax

- Variables are uppercase
- Constants, predicates are lowercase
- List syntax:
  - \([1, 2, 3]\)
  - \([\text{head} \mid \text{tail}]\)
- Program consists of
  - Facts, rules, and goals

Facts

female(shelley).
male(bill).
female(mary).
male(jake).
father(bill, jake).
father(bill, shelley).
mother(mary, jake).
mother(mary, shelley).

Rules

parent(X, Y) :- mother(X, Y).
president(X, Y) :- father(X, Y).
grandparent(X, Z) :-
  parent(X, Y), parent(Y, Z).
sibling(X, Y) :-
  mother(M, X), mother(M, Y).
sibling(X, Y) :-
  father(F, X), father(F, Y).
ancestor(X, Y) :-
  father(F, X), parent(F, Y).
ancestor(X, Y) :-
  parent(X, Z), ancestor(Z, Y).
Queries

?- father(bill, jake).
   yes
?- father(X, jake).
   X = bill
   yes
?- father(bill, X).
   X = jake
; X = shelley
   yes

Another Example

% Sir Bedevere’s reasoning in Monty Python and
% the Holy Grail to prove that girl is a witch.

witch(X) :- burns(X), woman(X).
woman(girl).
burns(X) :- isMadeOfWood(X).
isMadeOfWood(X) :- floats(X).
floats(duck).
floats(Y) :- floats(X), !, sameWeight(X, Y).
sameWeight(duck, girl).
?- witch(girl).

Is the Girl a Witch?

witch(girl)
burns(girl), woman(girl)
isMadeOfWood(girl), woman(girl)
floats(girl), woman(girl)
floats(X), !, sameWeight(X, girl), woman(girl)
!, sameWeight(duck, girl), woman(girl)
sameWeight(duck, girl), woman(girl)
woman(girl)
success
List Processing Predicates

\% member(X, L) <- X is a member of L
\% append(X, Y, Z) <- Z is list consisting of Y appended to X

member(X, [X|_]).
member(X, [_|Ys]) :- member(X, Ys).

append([], Y, Y).
append([X|Xs], Y, [X|Zs]) :-
    append(Xs, Y, Zs).

Functional Queries

?- member(c, [a,b,c,d,e]).
   yes
?- member(f, [a,b,c,d,e]).
   no
?- append([a,b], [c,d,e], X).
   X = [a,b,c,d,e]
   yes

Relational Queries

?- member(e, [a,b,c,d,X]).
   X = e
   yes
?- append(X, [c,d,e], [a,b,c,d,e]).
   X = [a,b]
   yes
?- append([a,b], Y, [a,b,c,d,e]).
   Y = [c,d,e]
   yes
Relational Queries

?- append(X, Y, [a,b,c,d,e]).
  X = [], Y = [a,b,c,d,e]
  \ X = [a], Y = [b,c,d,e]
  \ X = [a,b], Y = [c,d,e]
  yes
?- member(X, [a,b,c]), member(X, [c,d]).
  X = a
  yes

Trace of Prolog Program

?- member(X, [a,b,c]), member(X, [c,d]).
%
% first attempt
% choice point: X = a
member(a, [c,d])
member(a, [d])
member(a, [])
%
% fails

Trace of Prolog Program

% backtrack to choice point
% second attempt
member(X, [b,c]), member(X, [c,d])
%
% choice point: X = b
member(b, [c,d])
member(b, [d])
member(b, [])
%
% fails
Trace of Prolog Program

% backtrack to last choice point
member(X, [c]), member(X, [c,d])
% choice point: X = c
member(X, [c,d])
% succeeds: X = c

Cut

- Prevents backtracking
- Cuts off previous choice points

floats(duck).
floats(X) :-
    floats(Y), !, sameWeight(X, Y).

; only works for functional queries
member(X, [X,_,]) :- !.
member(X, [_,Ys]) :- member(X, Ys).

Arithmetic

factorial(0, 1).
factorial(N, Value) :-
    N > 0, K is N – 1, factorial(K, Kfact),
    Value is Kfact * N, !.
Execution of Prolog Programs

- Prove that goal is satisfiable
- Search of facts/rules is top-down
- Execution of sub-goals is left to right
- Closed-world assumption:
  - anything not in database is false
- Negation not equivalent to logical not
- Integer calculation, I/O don't fit well into logical proof search

Applications of Prolog

- Relational database queries
- Expert systems
- Parsing of context-free languages
- Natural language processing
- Teaching programming, as early as in grade school
- SICStus Prolog: flight reservation