
Special Topics in OpenGL

Rasterization

What is Rasterization?

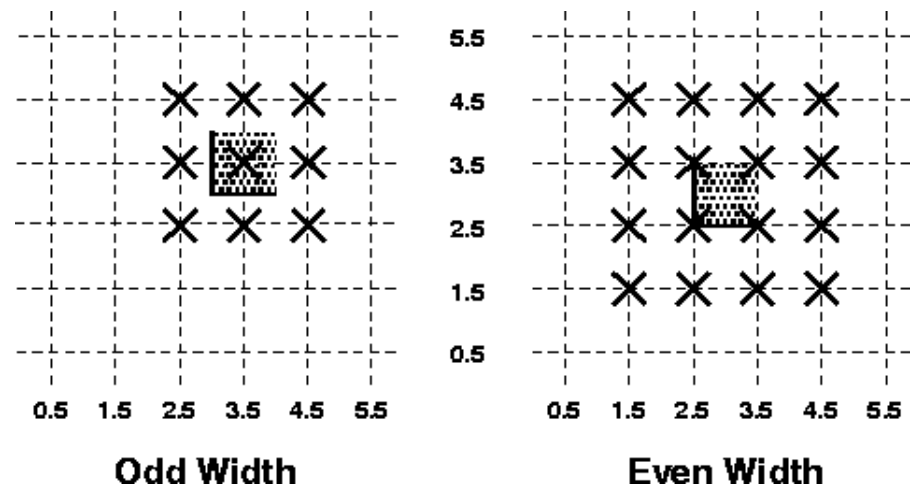
- Is a process by which a primitive is converted to a 2D image
 - Determine which squares of an integer grid in window coordinates are occupied by the primitive
 - Assign a color and a depth value to each square
- A grid square along with its assigned color and depth is called a fragment
- The results of the process are passed to the next stage of per-fragment operations

Point Rasterization

- Point is rasterized as a single fragment truncating its (x_w, y_w) coordinates to integers
- For wide points, fragment centers are at

$$\left(\lfloor x_w \rfloor + \frac{1}{2}, \lfloor y_w \rfloor + \frac{1}{2} \right) \quad \text{(Odd)}$$

$$\left(\left\lfloor x_w + \frac{1}{2} \right\rfloor, \left\lfloor y_w + \frac{1}{2} \right\rfloor \right) \quad \text{(Even)}$$



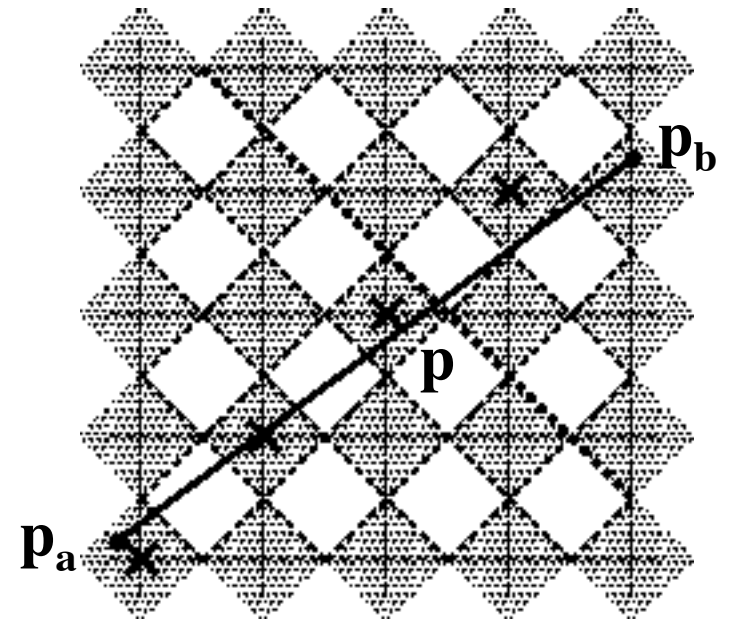
- The data associated with each rasterized fragment is the same as that of the vertex

Line Segment Rasterization

- Diamond-exit rule to determine the fragments produced by rasterization
- Specify the data associate with each rasterized fragment

$$f = \frac{(1-t)f_a/w_a + tf_b/w_b}{(1-t)/w_a + t/w_b}$$

$$\text{Where } t = \frac{(p - p_a) \cdot (p_b - p_a)}{|p_b - p_a|^2}$$

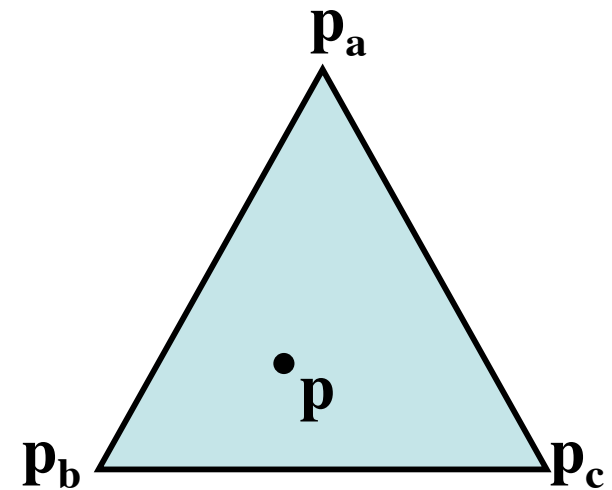


Polygon Rasterization

- Point sampling
 - Rasterized fragment centers lie inside the projected polygon
 - If two or more polygons share the same fragment, it is rasterized by one of them
- Specify the data associated with each rasterized fragment

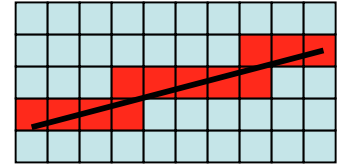
$$f = \frac{af_a / w_a + bf_b / w_b + cf_c / w_c}{a / w_a + b / w_b + c / w_c}$$

$p = ap_a + bp_b + cp_c$ defines any point in a triangle with barycentric coordinates (a , b , and c)



Antialiasing

- Lines (nearly horizontal or vertical) appear zagged
- Reducing this zagginess is called antialiasing
 - Calculates a coverage value for each fragment based on the fraction of the pixel square on the screen that it would occur
 - Multiplies the fragment's alpha by its coverage
 - Use the resulting alpha to blend the fragment with the corresponding pixel already in the frame buffer
- Antialiasing points or lines or polygons
 - Pass `GL_POINT_SMOOTH` or `GL_LINE_SMOOTH` or `GL_POLYGON_SMOOTH` to `glEnable()`
 - Enable blending



Example: Aliased and antialiased lines

Framebuffer

What is Framebuffer

- Each fragment has coordinate data which correspond to a pixel, as well as color and depth values
- Buffers (storages) to hold the various kinds of information of pixels
- OpenGL implementation supports the following buffers
 - Color buffer
 - Depth buffer
 - Stencil buffer
 - Accumulation buffer

The buffers are used to perform special tasks before pixels are finally written to the viewable color buffer
- A collection of these buffers is called framebuffer

Color Buffers

- Color buffers are the ones to which you draw
 - They contain RGBA data
- Stereoscopic viewing needs left and right color buffers for the left and right stereo images
- Double-buffered systems have front and back color buffers
- Non-displayable auxiliary color buffers can be used
- Minimum requirement is a front-left color buffer

Other Buffers

- Depth buffer (z-buffer):
 - Stores a depth value for each pixel
 - Depth is usually measured in terms of distance to the eye
 - Used for a hidden-surface removal
- Stencil buffer:
 - Stores the information to restrict drawing to certain portions of the screen
- Accumulation buffer:
 - Holds RGBA color data for accumulating a series of images into a final, composite image
 - When accumulation is finished, the result is copied back into the color buffer for viewing
 - Used for scene antialiasing, motion blur, simulating depth of field, and calculating soft shadows

Clearing Buffers

- Clearing the screen (or any of the buffers) is expensive
 - Hardware can clear more than one buffer at once
- First, specify the current clearing values for each buffer

```
void glClearColor(GLclampf red, GLclampf green, GLclampf blue,  
                 GLclampf alpha);  
void glClearDepth(GLclampf depth);  
void glClearStencil(GLuint s);  
void glClearAccum(GLclampf red, GLclampf green, GLclampf blue,  
                 GLclampf alpha);
```
- Then issue a single clear command

```
void glClear(GLbitfield mask);
```

mask is the bitwise logical OR of some combination of
GL_COLOR_BUFFER_BIT, GL_DEPTH_BUFFER_BIT,
GL_STENCIL_BUFFER_BIT, and GL_ACCUM_BUFFER_BIT

Color Buffers for Writing and Reading

- **void glDrawBuffer(GLenum *mode*);**
 - Selects the color buffers enabled for writing or clearing
 - *mode* can be GL_FRONT, GL_BACK, GL_LEFT, GL_RIGHT, GL_FRONT_LEFT, etc.
 - Default mode is GL_FRONT for single-buffered contexts and GL_BACK for double-buffered contexts
- **void glReadBuffer(GLenum *mode*);**
 - Selects the color buffer enabled as the source for reading pixels

Masking Buffers

- Sets the masks used to control writing into the indicated buffers
- `void glColorMask(GLboolean red, GLboolean green, GLboolean blue, GLboolean alpha);`
 - The *red*, *green*, *blue* and *alpha* values control whether corresponding component is written
- `void glDepthMask(GLboolean flag);`
 - *flag* is `GL_TRUE` for writing in depth buffer
- `void glStencilMask(GLuint mask);`
 - *mask* = 1 for writing the bit

Testing and Operating on Fragments

- After fragments are generated, several processing stages occur determining how and whether a given fragment is drawn as pixel into the framebuffer
- Set of tests:
 - Scissor test
 - Alpha test
 - Depth test
 - Stencil test
 - Blending
 - Dithering
 - Logical operation

Scissor Test

- `void glScissor(GLint x, GLint y, GLsizei width, GLsizei height);`
 - Sets the location and size of the scissor rectangle or box
 - By default, the rectangle matches the window
 - Drawing occurs only inside the rectangle: pixels lying inside the rectangle pass the scissor test
 - Needs enabling
`glEnable(GL_SCISSOR_TEST);`

Alpha Test

- **void glAlphaFunc(GLenum *func*, GLclampf *ref*);**
 - Sets the reference value and comparison function for the alpha test
 - In RGBA mode, a fragment is accepted or rejected by the alpha test on its alpha value
 - By default, *ref* is zero, and *func* is `GL_ALWAYS`
 - *func* can be `GL_ALWAYS`, `GL_NEVER`, `GL_LESS`, `GL_EQUAL`, `GL_LEQUAL`, `GL_GEQUAL`, `GL_GREATER` or `GL_NOTEQUAL`
 - Needs enabling
`glEnable(GL_ALPHA_TEST);`

Depth Test

- **glDepthFunc(GLenum *func*);**
 - Sets the comparison function for the depth test
 - An incoming fragment passes the depth test if its z value has specified relation to the value already stored in the depth buffer
 - By default, *func* is `GL_LESS`

Pixels with larger depth-buffer values are overwritten by pixels with smaller values
 - *func* can be `GL_ALWAYS`, `GL_EQUAL`, `GL_GREATER`, etc.
 - Needs enabling
`glEnable(GL_DEPTH_TEST);`

Stencil Test

- The stencil test takes place only if there is a stencil buffer
 - It compares a reference value with the value stored at a pixel in the buffer
 - Depending on the test result, the value in the stencil buffer is modified
- `void glStencilFunc(GLenum func, GLint ref, GLuint mask);`
 - Sets the comparison *func*, reference *ref* and *mask* for the test
Comparison applies to those bits for which bits of the mask are 1
 - *func* can be `GL_ALWAYS`, `GL_LESS`, etc.
 - Needs enabling: `glEnable(GL_STENCIL);`
- `glStencilOp(GLenum fail, GLenum zfail, GLenum zpass);`
 - Specifies how the data in the stencil buffer is modified when a fragment passes or fails the stencil test
 - *fail*, *zfail*, *zpass* can be `GL_KEEP`, `GL_ZERO`, `GL_REPLACE`, `GL_INCR`, `GL_DECR`, `GL_INVERT`

fail = failed stencil test; *zfail* = failed z test; *zpass* = passed z test

Other Operations

- Blending
 - Combines the incoming fragment's R, G, B and A values with those of the pixel already stored at the location
- Dithering
 - Dither the values of red, green and blue on neighboring pixels for the perception of a wide range of colors
Needs enabling with `GL_DITHER`
- Logical Operations
 - Are applied between the incoming fragment's color and the color stored at the corresponding location in the framebuffer
 - The result replaces the value in the framebuffer for that fragment
`void glLogicOp(GLenum opcode);`
opcode can be `GL_CLEAR`, `GL_COPY`, `GL_AND`, etc
Needs enabling with `GL_COLOR_LOGIC`

Blending

What Blending?

- Combining colors from a source (incoming fragment) and destination (the corresponding pixel) to achieve such effects as making objects appear translucent
- The source and destination factors are RGBA quadruplets:
 - (S_r, S_g, S_b, S_a) and (D_r, D_g, D_b, D_a)
- Blended RGBA values are
 - $(R_s S_r + R_d D_r, G_s S_g + G_d D_g, B_s S_b + B_d D_b, A_s S_a + A_d D_a)$

Where (R_s, G_s, B_s, A_s) and (R_d, G_d, B_d, A_d) are the RGBA values of source and destination

How to Specify?

- `void glBlendFunc(GLenum sfactor, GLenum dfactor);`
 - Controls how color values in the fragment being processed (the source) are combined with those already stored in the framebuffer (the destination)
 - *sfactor* (*dfactor*) indicates how to compute a source (destination) blending factor
 - GL_ONE: (1,1,1,1)
 - GL_SRC_ALPHA: (As,As,As,As)
 - GL_ONE_MINUS_SRC_ALPHA: (1,1,1,1)-(As,As,As,As)
 - Needs enabling
`glEnable(GL_BLEND);`

3D Blending with the Depth Buffer

- For 3D objects, the appearance depends on whether you draw the polygons from back to front or from front to back
 - drawing order
- Consider the effect of the depth buffer in determining the order
 - If an opaque object hides other objects, eliminate the more distant objects
- If the translucent object is closer, blend it with the opaque object
- **Example: Sphere inside a Cube**

Animation

Pictures That Move

- Animation is an important part of computer graphics
- Seeing all sides of a mechanical part designed
- Learning to fly an airplane using a simulation
- Viewing molecular dynamics
- Viewing vector data

Motion = Redraw + Swap

- OpenGL provides double buffering (two color buffers)
 - One is displayed while the other is being drawn
 - When drawing of a frame is complete, the two buffers are swapped
 - Like a movie projector with only two frames in a loop
- `void glutSwapBuffers(void);`
 - Swap the viewable and drawable buffers
 - Waits until one frame is completely drawn and other is completely displayed
 - For a system with display refresh rate of 60 times per second, the fastest frame rate can be 60 frames per second
- `void glutInitDisplayMode(GLUT_DOUBLE | GLUT_RGB);`
 - Set double buffered window mode

Example: Solar System

```
void display (void) {
    glClear (GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
    glColor3f (1.0, 1.0, 1.0);
    glPushMatrix ();
    glRotatef (year, 0.0, 1.0, 0.0);
    glutSolidSphere (1.0, 80, 64);
    glTranslatef (2.0, 0.0, 0.0);
    glRotatef (day, 0.0, 1.0, 0.0);
    glutSolidSphere (0.2, 80, 64);
    glPopMatrix ();
    glutSwapBuffers ();
}
glutInitDisplayMode (GLUT_DOUBLE | GLUT_RGB);
```

- Sun is rotating about its own axis; planet is orbiting around the sun as well as rotating about its own axis
The graphics remain idle between the frames

Hidden-Surface Removal

Hidden Surface?

- In a scene composed of 3D objects, some of them might obscure all or parts of others
- The obscuring relationship changes with viewpoint and needs to be properly maintained
- Hidden-surface removal is elimination of parts of solid objects that are obscured by others
- Otherwise, the objects are drawn in the order the drawing commands appear in the code
- Hidden-surface removal increases performance

Use of Depth Buffer

- Use of depth buffer (*z-buffer*) to achieve hidden surface removal
- Graphical calculations convert each surface (before drawing) to a set of corresponding pixels on the window and also compute depth value for each pixel
- A comparison is done with the depth value already stored at that pixel to accept the pixel only if it has a smaller depth
- Color and depth information of the incoming pixel with greater depth is discarded

How to Specify?

- In void **glDepthFunc**(GLenum *func*);
Default value of *func* is used: GL_LESS used
`glEnable(GL_DEPTH_TEST);`
- **glutInitDisplayMode** (GLUT_RGB | GLUT_DEPTH);
- Before drawing, each time you need to clear the depth buffer and draw objects in any order
`glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);`
`glClear()` clears both color and depth buffers
- **Planet hides behind the sun in solar system example**

Drawing Pixel Data

Geometric Versus Pixel Data

- Rendering of geometric data (arrays of vertices)
 - points, lines, polygons
- Rendering of pixel data (arrays of pixels)
 - **Bitmaps**
 - Characters in fonts
 - Array of 0s and 1s(1 = the pixel is affected)
 - Serves as drawing mask for overlying another image
 - **Image data**
 - A photograph that is scanned or an image calculated by some program in memory by pixels or an image first drawn and then read back pixel by pixel
 - Several pieces of data per pixel (R,G,B,A values)
 - Simply overwrites in the framebuffer

Current Raster Position

- `void glRasterPos{234}{sifd}(TYPE x, TYPE y, TYPE z, TYPE w);`
 - Sets the current raster position where the next bitmap (or image) is to be drawn
 - The raster position coordinates are subject to the modelview and projection transformations in the same way as the vertex coordinates
- To specify the raster position directly in the screen coordinates, only 2D version of transformations need to be specified

Drawing Bitmaps

- void **glBitmap**(GLsizei *width*, GLsizei *height*, GLfloat x_{bo} , GLfloat y_{bo} , GLfloat x_{bi} , GLfloat y_{bi} , const Glubyte **bitmap*);
 - Draws the bitmap specified by *bitmap*
 - *Width and height* define size of the bitmap
 - Subscript *bo* means the origin of the bitmap
 - Subscript *bi* means increment to the current raster position after the bitmap is rasterized

Manipulating Images

- void **glReadPixels**(GLint *x*, GLint *y*, GLsizei *width*, GLsizei *height*, GLenum *format*, GLenum *type*, GLvoid **pixels*)
 - Reads pixel data from the *specified* framebuffer rectangle and stores data in the array pointed by *pixels*
 - *format* can be GL_RGBA, GL_RED, GL_ALPHA, GL_DEPTH_COMPONENT
 - *type* can be s, u, i, f, etc.
- void **glDrawPixels**(GLsizei *width*, GLsizei *height*, GLenum *format*, GLenum *type*, GLvoid **pixels*)
 - Draws a rectangle of pixel data with dimensions *width* and *height*
 - Pixel rectangle has its lower-left corner at the current raster position
- void **glCopyPixels**(GLint *x*, GLint *y*, GLsizei *width*, GLsizei *height*, GLenum *buffer*)
 - Copies pixel data from the specified framebuffer rectangle
 - Buffer can be GL_COLOR, GL_DEPTH, GL_STENCIL

Example: Drawing Image

- Make a checkerboard image
- Define raster position
- Draw an pixel rectangle of the image

Texture Mapping

What is Texture Mapping?

- Gluing an image (such as scanned photograph) to a polygon
 - Bricks on wall
 - Ground in flight simulation
 - Vegetation
- Textures are rectangular arrays of data (colors, luminance)
 - Individual values are called texels
- Textures can be manipulated with transformations
 - Repeat textures in different directions to cover the surface
 - Apply textures in different shapes and sizes

Steps in Texturing

- Create a texture object and specify a texture for the object
- Indicate how the texture is to be applied to each pixel
- Enable texture mapping
- Draw the scene by supplying both texture and geometric coordinates

Sample Example

- Checkboard texture is generated
`makeCheckImage()`
- All texture mapping initialization occurs in **init()**
`glGenTextures(1, &texName);`
`glBindTexture(GL_TEXTURE_2D, texName);`
- Single, full resolution texture map is specified
`glTexImage2D(GL_TEXTURE_2D, 0, GL_RGBA, checkImageWidth,
checkImageHeight, 0, GL_RGBA, GL_UNSIGNED_BYTE, checkImage);`
- Specify how the texture to be wrapped and how the colors are to be filtered if there is not an exact match between texels and pixels
`glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_S, GL_REPEAT);`
`glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, GL_NEAREST);`

More on Example

- In **display**(void), texture is turned on
`glEnable(GL_TEXTURE_2D);`
- Drawing mode is set so as to draw the textured polygons using the colors from the texture map
`glTexEnvf(GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE, GL_REPLACE);`
- Two polygons are drawn by specifying texture coordinates along with vertex coordinates
`glTexCoord2f(0.0,0.0); glVertex3f(-2.0,-1.0,0.0);`
.....
- Texture is finally turned off
`glDisable(GL_TEXTURE_2D);`

3D Textures

- 3D textures are used in scientific visualization
 - e.g. volume rendering
- Defining a 3D texture:
 - `glTexImage3D(GL_TEXTURE_3D, 0, GL_RGB, iWidth, iHeight, iDepth, 0, GL_RGB, GL_UNSIGNED_BYTE, image);`
- Replace all or some of the texels of a 3D texture
- Using compressed texture images
- Mipmaps: Multiple levels of detail
- Filtering
- Texture objects
- Texturing functions

Display Lists

What and Why Display List?

- In many cases, you may need to execute the same set of OpenGL commands multiple times
- Drawing a tricycle:
 - Two wheels on the back are the same size but are offset from each other. The front wheel is larger and in a different location
 - An efficient way to render the wheels on the tricycle is store the geometry for one wheel in a list and then execute the list three times by setting the appropriate modelview matrix each time before executing the list
- Several other examples: Solar system, molecular dynamics

What and Why Display List?

- A display list is a group of OpenGL commands that have been stored for later execution
- You can define the geometry and/or state changes once and execute them multiple times by providing a number that uniquely specifies the display list
- Display lists improve performance by caching commands which are reused many times

Naming and Creating a Display List

- Each display list is identified as a unique, system-generated integer index or ID
- **GLuint glGenLists (GLsizei *range*);**
 - Allocates *range* number of contiguous, previously unallocated display list indices
 - The integer returned is the index that marks the beginning of a contiguous block of empty display list indices

If returned integer is n , then indices $n, n+1, \dots, n + range - 1$ are available

`listIndex = glGenLists(1);`

Generates one new display list ID and store it in variable `listIndex`

glIsList(GLuint *list*) to check whether a specific index is in use. It returns `GL_TRUE` if the *list* is already used

glDeleteLists(GLuint *list*, GLsizei *range*) to delete *range* display lists starting at the index specified by *list*

Naming and Creating a Display List

- `void glNewList(GLuint list, GLenum mode);`
 - Specifies the start of a display list.
 - The argument *list* is a nonzero positive integer that uniquely identifies the display list
 - The possible values for *mode* are `GL_COMPILE` and `COMPILE_EXECUTE`
- `void glEndList(void);`
 - Marks the end of a display list

```
glNewList (listIndex, GL_COMPILE);
```

```
.....
```

```
glEndList();
```

Executing a Display List

- **Void glCallList(GLint *list*);**
 - Executes the display list specified by *list* which is the index for the display list
 - Commands in the display list are executed, just as if they were issued
- You can execute the same display list many times
- You can mix display lists and immediate-mode graphics

Example

- The display list contains OpenGL commands to draw a triangle
- The display list is executed multiple times
- A rectangle is drawn in immediate mode.

Hierarchical Display Lists

- A hierarchical display list executes another display list in it by calling **glCallList()** between a **glNewList()** and **glEndList()** pair

➤ A display list to render a tricycle:

```
glNewList(listIndex, GL_COMPILE);  
    glCallList(handlebars);  
    glCallList(frame);  
    glTranslatef(1.0,0.0,0.0);  
    glCallList(wheel);  
    glTranslatef(3.0,0.0,0.0);  
    glCallList(wheel);  
    glTranslatef(3.0,0.0,0.0);  
    glScalef(1.5,1.5,1.5);  
    glCallList(wheel);  
glEndList();
```

Multiple Display Lists

- `void glListBase(GLuint base);`
 - Specifies the offset that's added to the display-list indices in `glCallLists()` to obtain the final display-list indices
- `void glCallLists(GLsizei n, GLenum type, const GLvoid *lists);`
 - Executes *n* display lists
 - **lists* is a pointer that points to an array of offsets
 - Nesting level of display lists is at least 64

Managing State Variables

- A display list can contain calls that change the value of OpenGL state variables
- The changes persist after execution of the display list is completed
- Use **glPushAttrib()** to save a group of state variables and **glPopAttrib()** to restore the values later
- Use **glPushMatrix()** and **glPopMatrix()** to save and restore the current matrix

Selection

Interactive Applications

- Allows user to select a region of the scene or pick an object drawn on the screen
- Selection mode
 - First draw scene, then use selection mode, and redraw the scene
 - Screen remains frozen while OpenGL is in selection mode
 - On exiting from selection mode, OpenGL returns a list of primitives that intersect the viewing volume
 - Each primitive within the viewing volume causes a selection hit

Basic Steps

- Specify the array to be used for the returned hit records with **glSelectBuffer()**
- Enter selection mode by specifying GL_SELECT with **glRenderMode()**
- Initialize the name stack using **glInitNames()**
- Define viewing volume to be used for selection
- Exit selection mode and process the hit records

Commands

- **void glSelectBuffer(GLsizei size, GLuint **buffer*);**
 - Specifies the array to be used for the returned selection data
 - *buffer* is a pointer to the array of the given *size*
- **void glRenderMode(GLenum *mode*);**
 - Controls whether the application is in rendering, selection, or feedback mode
 - *mode* is GL_RENDER, GL_SELECT or GL_FEEDBACK
 - *mode* remains unchanged until glRenderMode() is called again with different argument

Creating the Name Stack

- `void glInitNames(void);`
 - Clears the name stack so that it's empty
- `void glPushName(Gluint mode);`
 - Pushes name onto the name stack
 - The stack contain at least 64 names
- `void glPopName(void);`
 - Pops one name off the top of the name stack
- `void glLoadName(GLuint name);`
 - Replaces the value on the top of the name stack with name

Hit Record

- A primitive that intersects the viewing volume causes a selection hit
- OpenGL writes a hit record into the selection array if there is a hit
- Each hit record consists of the following items
 - Number of names on the name stack when the hit is occurred
 - Minimum and maximum window coordinate depth (z) values of all selected primitives
 - Contents of the name stack at the time of the hit

Picking

- Use selection mode to determine if the object are picked
- Picking is triggered by an input device (mouse click)
- Use a special picking matrix in conjunction with the projection matrix

void **glPickMatrix**(GLdouble *x*, GLdouble *y*, GLdouble *width*, GLdouble *height*, GLint *viewport*[4]);

- Creates a projection matrix that restricts drawing to a small region of the viewport and multiplies that matrix onto current matrix stack
- *x,y* define the center of picking region (or cursor location)
- *width and height* define the size of the picking region
- *viewport[]* indicates the current viewport boundaries.

Evaluators

What is Evaluators?

- Provide way to describe curves and surfaces by using few parameters or control points
- Use a polynomial mapping to produce vertex, normal, and texture coordinates, and colors
- Precision and storage efficient

One-Dimensional Evaluators

A vector-valued function (called Bezier curve) of one variable is

$$C(u) = [X(u), Y(u), Z(u)] = \sum_{i=0}^n B_i^n(u) P_i$$

Example:
distance traveled
by a body as a
function of time

Where P_i represent a set of n control points (3D) for vertices, colors or normals, and

$$B_i^n(u) = \binom{n}{i} u^i (1-u)^{n-i}$$

is i^{th} Bernstein polynomial of degree n

Domain for variable u is $[0.0, 1.0]$.

But if it is $[u_1, u_2]$, the function at u is evaluated as

$$C\left(\frac{u - u_1}{u_2 - u_1}\right)$$

Defining

- `void glMap1{fd}(GLenum target, TYPE u1, TYPE u2, GLint stride, GLint order, const TYPE *points);`

- Defines 1D evaluator

- *target*: what control point represent and how many values need to be supplied in points

GL_MAP1_VERTEX_3, GL_MAP1_COLOR_4, GL_MAP1_NORMAL

- *u*₁ and *u*₂: range for variable *u*

- *stride*: an offset value between the beginning of one control point and the beginning of the next

- *order*: *degree* + 1

`glMap1f(GL_MAP1_VERTEX_3, 0.0, 1.0, 3, 4, &cntrlpoints[0][0]);`
`glEnable(GL_MAP1_VERTEX_3);`

Evaluating

- `void glEvalCoord1{fd}(TYPE u);`
 - Causes evaluation of the enabled 1D maps
 - u is the domain coordinate
 - Call does not affect the current values for color and normal vectors
 - Call appears between `glBegin()` and `glEnd()` pair
- More than one evaluator can be evaluated at a time
 - Define and enable both `GL_MAP1_VERTEX_3` and `GL_MAP1_COLOR_4`
so that a single call to `glEvalCoord1()` generate both position and color along the curve

Defining Evenly Spaced u Values

- Use a 1D grid of u values for evaluation of function
- `void MapGrid1{fd}(GLint n , TYPE u_1 , TYPE u_2);`
 - Define a grid that goes from u_1 and u_2 in n steps, which are evenly spaced
- `void glEvalMesh1(GLenum $mode$, GLint p_1 , GLint p_2);`
 - Applies currently defined map grid to all enabled evaluators
 - Mode: `GL_POINT` or `GL_LINE`
 - p_1 and p_2 defines the range of steps

Two-Dimensional Evaluators

A vector-valued function (called Bezier surface) of two variables (u and v) is

$$C(u,v) = [X(u,v), Y(u,v), Z(u,v)] = \sum_{i=0}^n \sum_{j=0}^m B_i^n(u) B_j^m(v) P_{ij}$$

Where P_{ij} represents a set of $m*n$ control points (3D), and B 's are Bernstein polynomials

Procedure to use 2D evaluators:

1. Define evaluator with **glMap2()**
2. Enable them by passing appropriate value to **glEnable()**
3. Invoke them either by **glEvalCoord2()** between **glBegin()** and **glEnd()** pair or

By specifying and applying a mesh with **glMapGrid2()** and **glEvalMesh2()**

2D Evaluators Command

- Void **glMap2**{fd}(GLenum *target*, TYPE *u*₁, TYPE *u*₂, GLint *ustride*, GLint *uorder*, TYPE *v*₁, TYPE *v*₂, GLint *vstride*, GLint *vorder*, const TYPE **points*);
- void **glEvalCoord2**{fd}(TYPE *u*, TYPE *v*);
- void **glMapGrid2**{fd}(GLint *nu*, TYPE *u*₁, TYPE *u*₂, GLint *nv*, TYPE *v*₁, TYPE *v*₂);
void **glEvalMesh2**(GLenum *mode*, GLint *i*₁, GLint *i*₂, GLint *j*₁, GLint *j*₂);
mode can be GL_POINT, GL_LINE, GL_FILL
- Normal to the surface can be computed with **glEnable**(GL_AUTO_NORMAL)

Tessellators, Quadrics, NURBs

Polygon Tessellation

- Process of subdividing non-simple polygons (such as concave polygons, polygons with holes, polygons with intersecting edges) into simple convex polygons
- Steps in polygon tessellation:
 - Create a new tessellation object with **gluNewTess()**
 - Use **gluTessCallback()** to register callback functions to perform operations during the tessellation
 - Specify tessellation properties by calling **gluTessProperty()**
 - Create and render tessellated polygons by the contours
 - Delete tessellation object with **gluDeleteTess()**

Quadrics

- Rendering spheres, cylinders, and disks:

- Quadric surfaces are defined by

$$a_1x^2 + a_2y^2 + a_3z^2 + a_4xy + a_5yz + a_6xz + a_7x + a_8y + a_9z + a_{10} = 0$$

- Steps in using quadrics object

- Use **gluNewQuadric()** to create a quadrics object

- Specifying rendering attributes with **gluQuadricOrientation()**, **gluQuadricDrawstyle()**, **gluQuadricNormals()**

- Invoke the rendering routines for different quadric objects: **gluSphere()**, **gluCylinder()**, **gluDisk()**

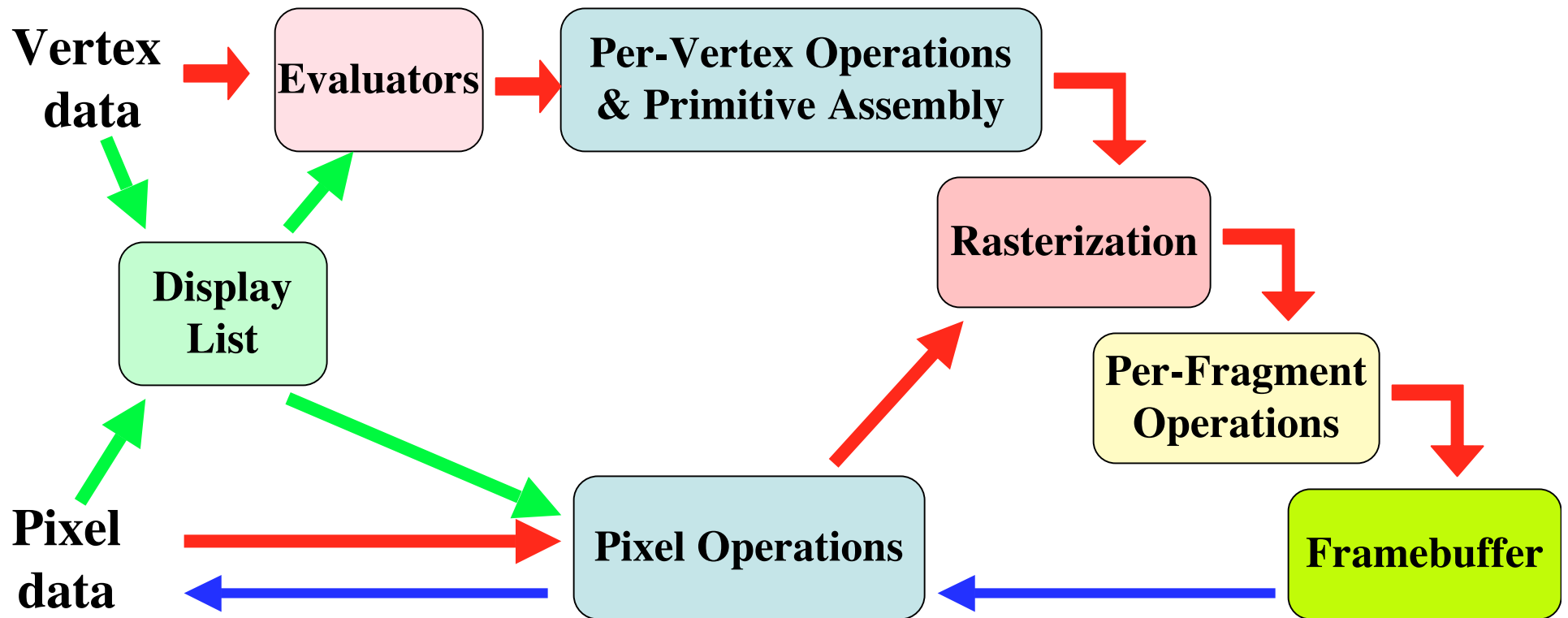
- Delete the quadric object with **gluDeleteQuadric()**

NURBS Interface

- GLU provides a NURBS (Non-Uniform-Rational-B-Spline) interfaces
- Steps to draw NURBS curves or surfaces
 - Use **gluNewNurbsRender()** to create a NURBS object
 - Start your curve or surface by calling **gluBeginCurve()** or **gluBeginSurface()**
 - Generate and render curve or surface with call to **gluNurbsCurve()** or **gluNurbsSurface()**
 - Call **gluNurbsProperty()** to choose rendering values such as number of polygons used
 - Call **gluNurbsCallback()** for different functions
 - Use lighting with **glEnable(GL_AUTO_NORMAL)**
 - Complete drawing with **gluEndCurve()** or **gluEndSurface()**

Summary

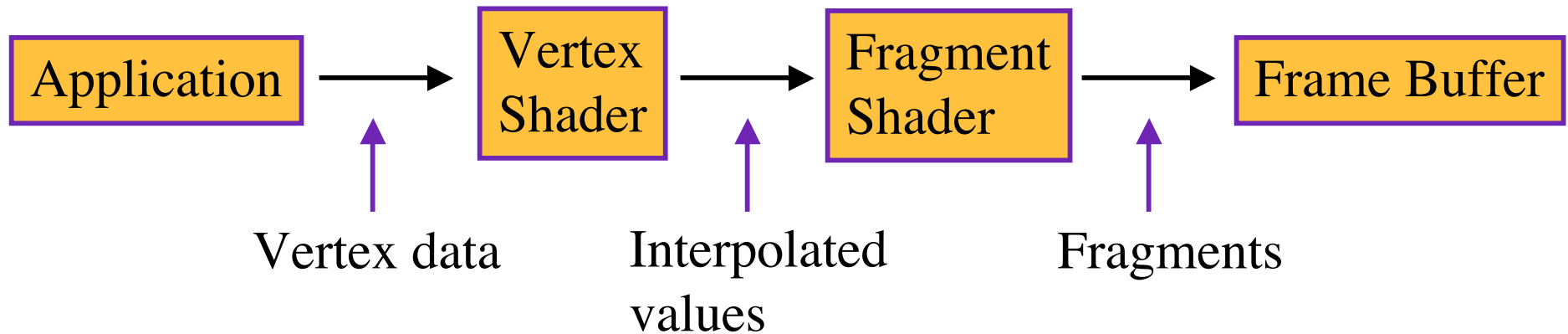
OpenGL Rendering Pipeline



Programmable Pipeline

- Graphics processors (GPUs) are programmable
 - Functionality of some of major units in the graphics pipeline can be altered by user programs which are executed in GPU
- Vertex shader
 - User programs to manipulate vertex properties
- Fragment shader
 - User programs to alter the processing of fragments
- Shading languages
 - The OpenGL Shading Language based on C
 - C for graphics: Cg

Programmable Pipeline: A Simple View



- All data (vertex, interpolated values and fragments) pass through a non-programmable part of the hardware
 - GPU registers store and transfer the data.

What Have We Covered?

- OpenGL Basics
 - OpenGL and related libraries, window management
- Drawing
 - Geometric primitive objects, vertex arrays, normal vectors, polygonal models of surfaces
- Viewing
 - Modelview transformations, projection transformations, viewport transformation, clipping, matrix stacks
- Color
 - Color perception, color functions, shading
- Lighting
 - Light sources, lighting models, material properties
- Special topics
 - Rasterization, framebuffer, animation, hidden-surface removal, blending, drawing pixel data, texture mapping, display lists, evaluators, selection
 - GPU programming