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# Scientific Visualization

# Scientific Datasets

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- Gaining insight into scientific data by representing the data by computer graphics
- Scientific data sources
  - **Computation**
    - Real material simulation/modeling (e.g., molecular dynamics simulation, electronic calculations)
    - Solving differential equations (e.g., fluid dynamics, electro-magnetic field)
    - Climate modeling
  - **Experiment**
    - Medical and biological: magnetic resonance imaging, computer tomography, confocal microscopy,
    - Other data: 3D laser scanner, atomic force microscopy, seismic tomography

# Data Challenges

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- Scale
  - MRI dataset:  $256^3 = 16$  MB per slice (each slice is 3 micron thick)  
How many slices to cover a particular organ
  - A million-atom simulation: 7 GB per step (each step is 1 femtosecond)  
How many steps to simulate a particular physical/chemical/biological phenomenon
- Dimensionality
  - 3D volume data
  - 4D space-time data
- Scalar, vector and tensor data
  - Density or temperature distribution
  - Data from flow dynamics
  - Stress-strain data

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# Scalar Visualization Techniques

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# Scalar Dataset

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- A single quantity that can be expressed as a function of position in space

$$S = S(x,y,z)$$

Array  $S$  represents data at discrete locations in space

- Describe the value at any continuous location by defining an interpolation function  $F(x,y,z)$
- Volume data (MRI, confocal, finite element modeling)
- Represented through regular grids  
If irregular grids, preprocessing of data to regular grid
- Each data element (cube or cell) often called **voxel**

# Different Rendering Techniques

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- Simple approaches
  - Symbols, Color mapping, Contour display
- Isosurface rendering
  - Marching cubes algorithm, Fast extraction approaches
- Implicit surfaces
  - Particle sampling, Dividing cubes algorithm, Shape function interpolation
- Volume slicing
  - Clipping, Sampling planes, Interactive clipping, Clip objects
- Volume rendering
  - Object-oriented, Image-oriented, Hybrid techniques

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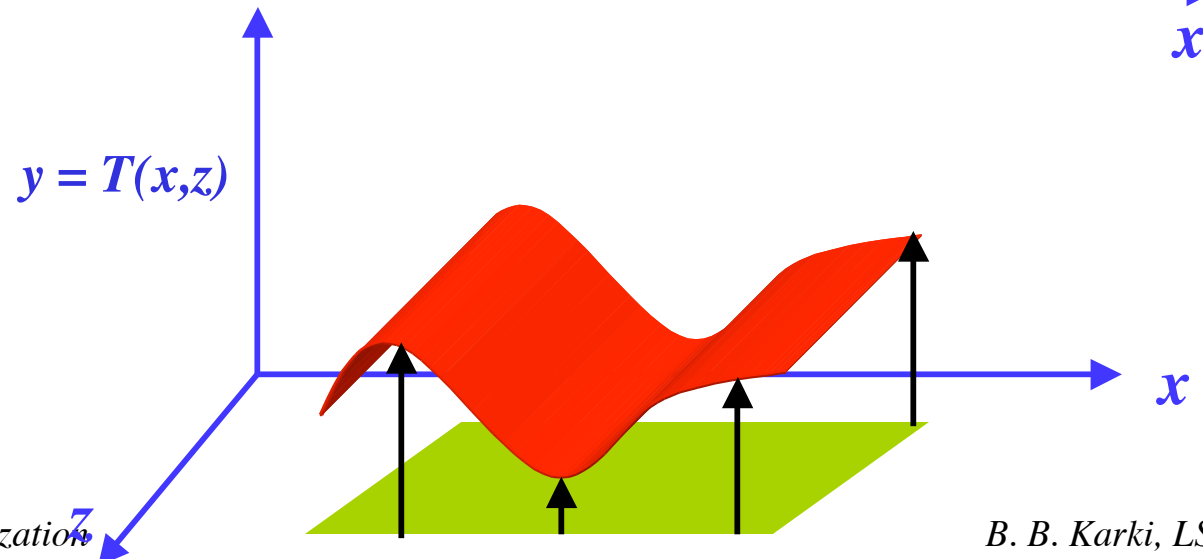
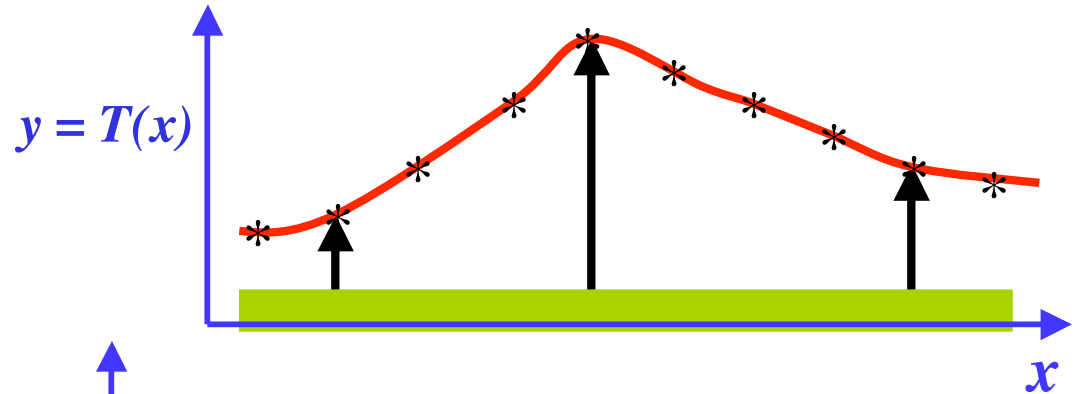
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# Simple Approaches

# Symbols or Off-Path Displays

- Useful for displaying one or two dimensional scalar data
  - Temperature distribution along a rod or on sheet

- Off-path displays





# Color Mapping: Lookup Table

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- Useful for scalar visualization in 1D, 2D or 3D
- Map scalar data to colors to display on the screen
- Lookup table:
  - Holds an array of colors (RGB components)
  - Scalar values serve as indices

For each  $s_i$ , there is index  $i$

$$i = n \left( \frac{s_i - \min}{\max - \min} \right)$$

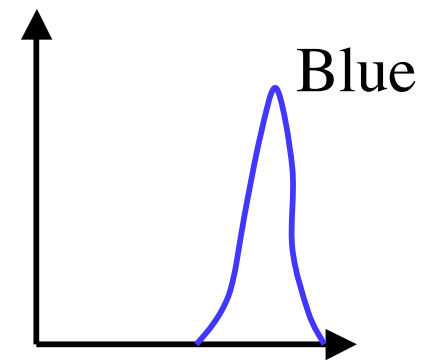
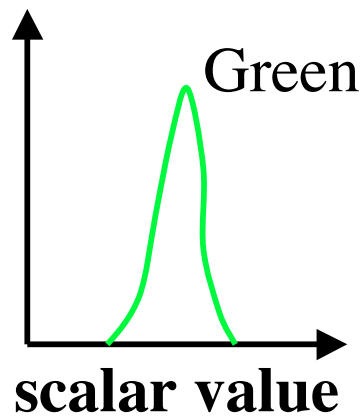
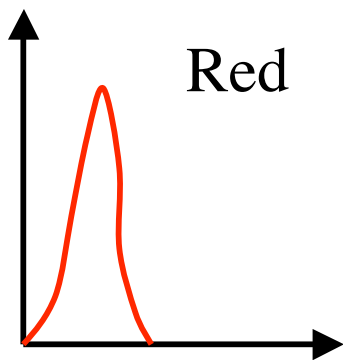
$i$

rgb0
rgb1
rgb2
.
.
rgbn-1

# Color Mapping: Transfer Function

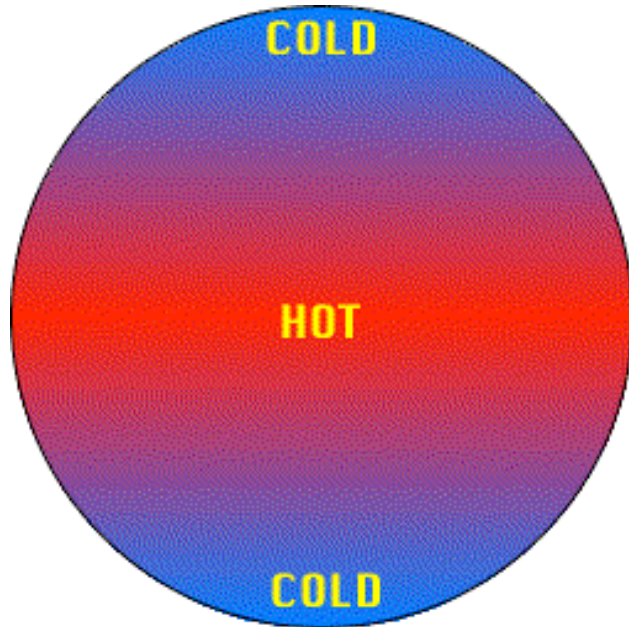
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- Transfer function
  - An expression that maps the scalar value into a color specification
  - Mapping to separate intensity values of R, G and B



- A lookup table is a discrete sampling of a transfer function

# Examples of Color Mapping

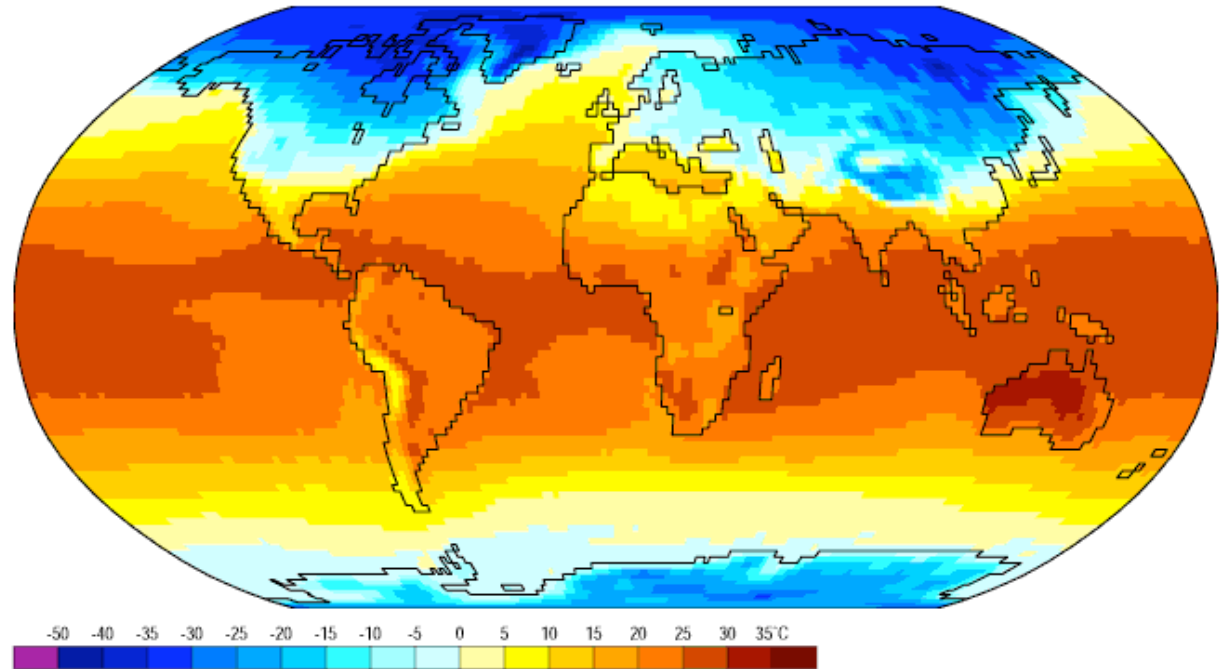


Simple latitudinal zonation temperature

### Mean January air temperature on the Earth's surface

Air Temperature

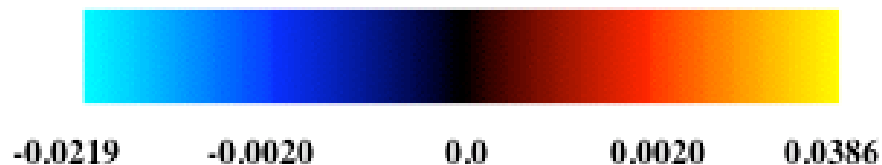
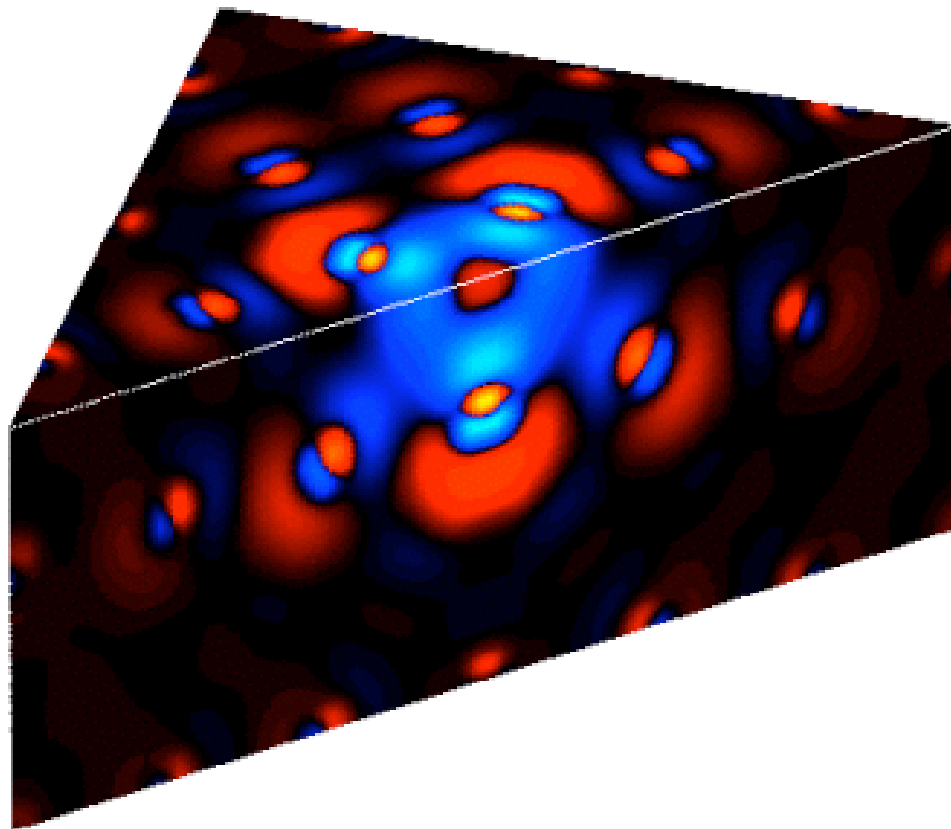
Jan



Data: NCEP/NCAR Reanalysis Project, 1959-1997 Climatologies

# Multiscale Color Mapping

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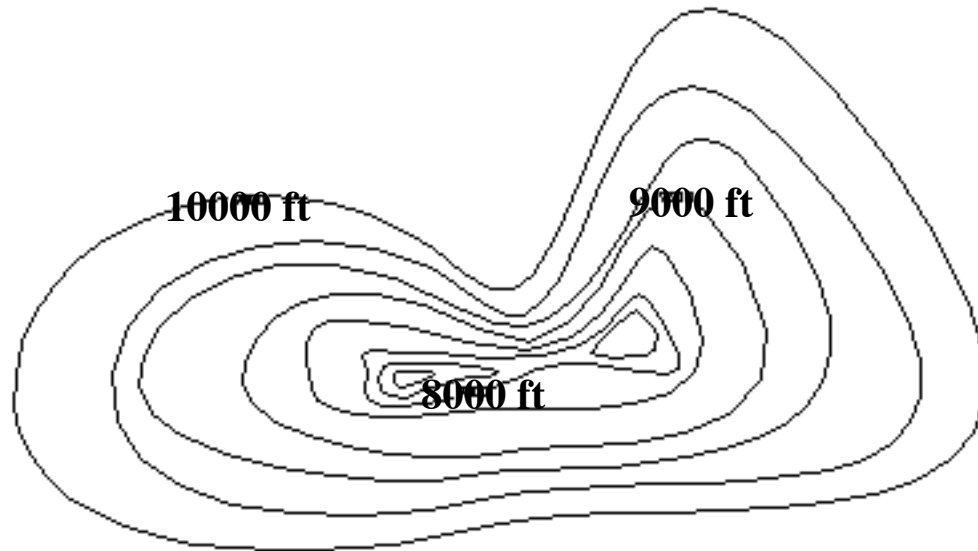
## Two-level mapping:

Fine-level scale uses the red and blue colors to represent the positive and negative differences with magnitude up to 0.002 (in units of  $\text{\AA}^{-3}$ )

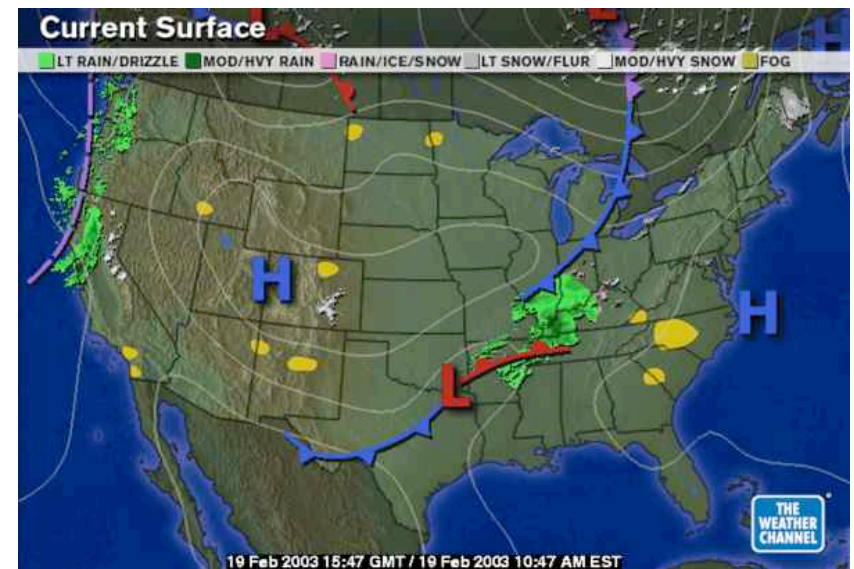
Coarse-level scale adds green color component to red and blue colors to map the positive and negative differences with magnitudes higher than 0.002.

# Contour Display

- Common method for displaying scalar data across a surface
- Contour lines: represent a constant value across the surface (isovalue lines)



**Topographic Map**



**Weather Map**

## 2D Contour Lines



# Edge ....

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- Once an edge with  $S_{iso}$  is found between vertices  $i$  and  $j$ , compute isovalue location along the edge by linear interpolation

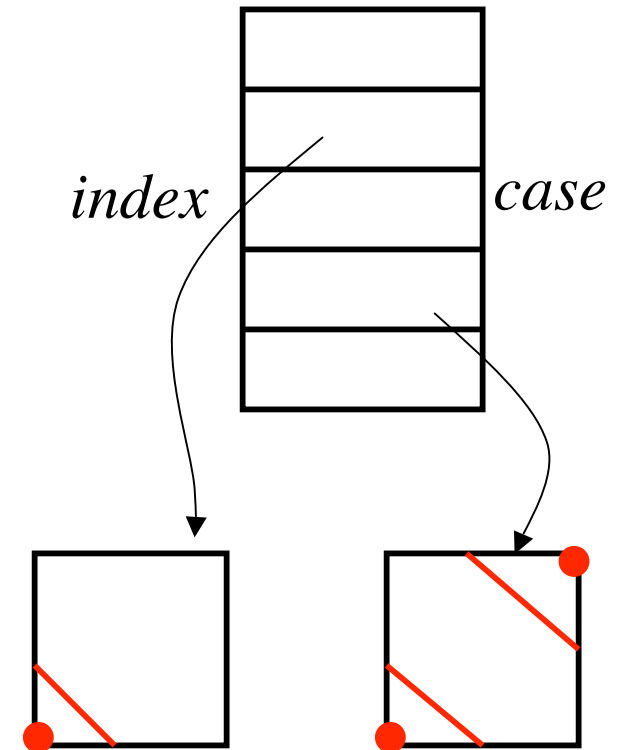
$$\begin{aligned}x &= x(i) + fac * (x(j) - x(i)) \\y &= y(i) + fac * (y(j) - y(i))\end{aligned}\quad \text{Where } fac = \left( \frac{S(j) - S_{iso}}{S(j) - S(i)} \right)$$

- This isovalue location will be the first point of the contour line  
Default location: mid point

- Examine each subsequent edge until the next edge containing an isovalue is found and repeat previous step
  - Connect these two points to form the contour segment
  - Use shape function to give isolines some curvature.

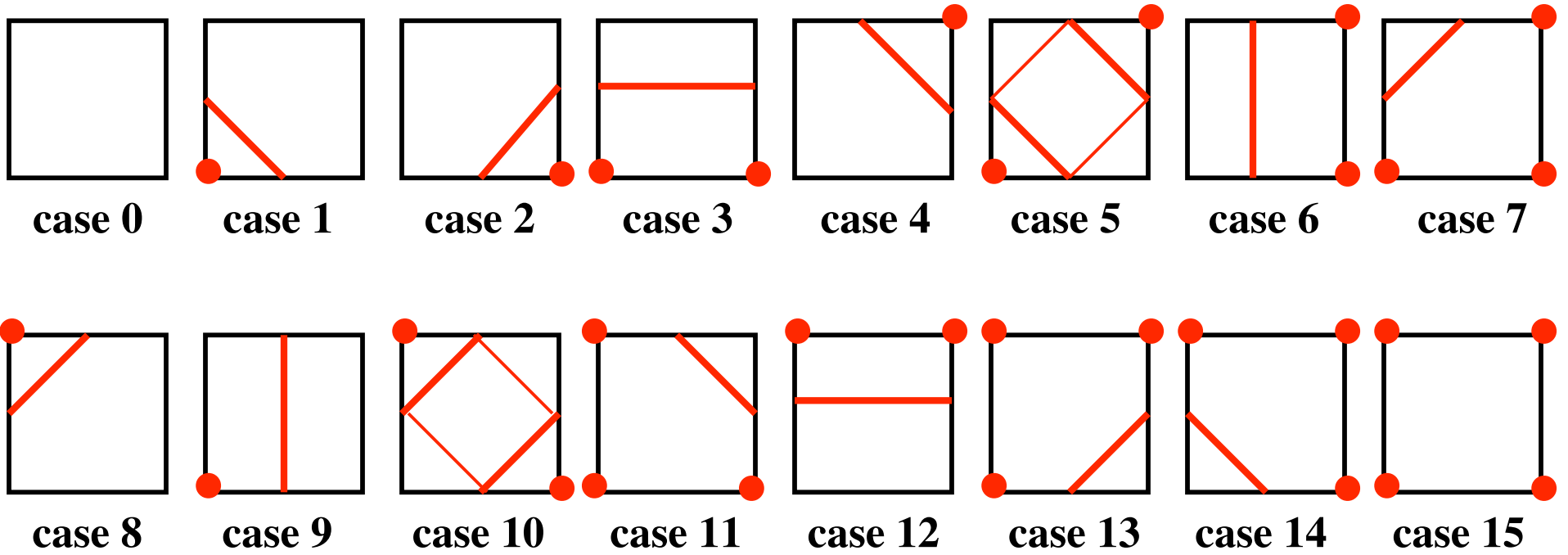
# Marching Squares Algorithm

- Select a square element or cell
  - Values at four corners
    - Below isovalue (marked)
    - Above isovalue (unmarked)
- Calculate inside or outside state of each vertex of the cell
- Determine the topology state of the cell by referring to a case table that has a list of all possible configurations
  - Each square is either inside, outside or intersected
  - 2D cell index: 4-bit,  $2^4$  (16) cases
- Calculate the contour location (via interpolation) for each edge in the case table
  - No or one intersection per edge





# Cases of 2D Cells (Squares)



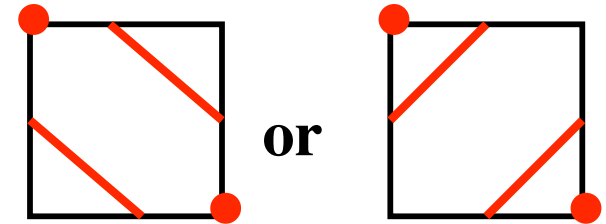
By complementary and rotational symmetries (equivalence), the number of the basic cases is reduced to 4



# 2D Ambiguous Cases

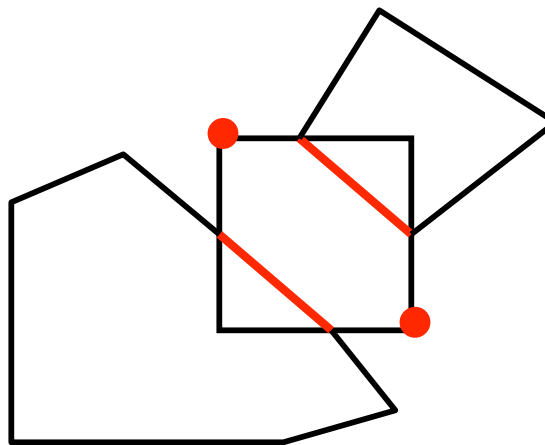
- Ambiguous cases:

➤ 5, 10

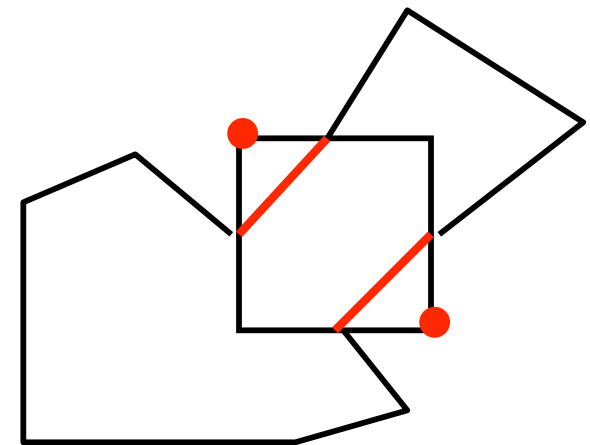


- Contour ambiguity arises when adjacent vertices in different states but diagonal vertices in the same state

- Break contour  
Join contour



**Break contour**



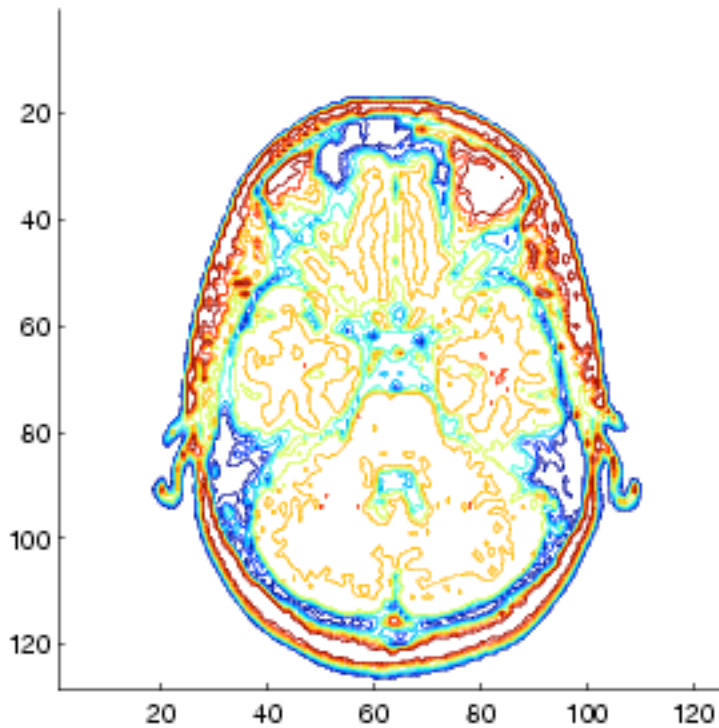
**Join contour**

- Both are valid

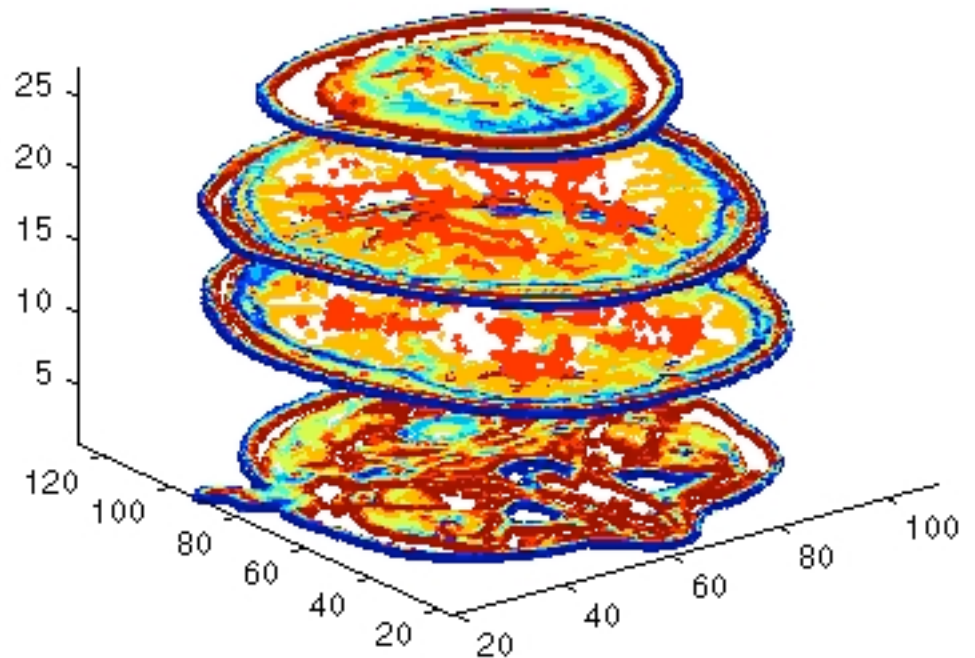
# Contour Lines of MRI Data

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Contour display of MRI data of a human head (single image and a stack of four images)



**2D contour**



**3D contour**